

# `Forecasting spatial structure of local precipitation extremes`

Bent Hansen Sass  
Danish Meteorological Institute  
Workshop 2020-IVMW-O  
November 2020

## OUTLINE

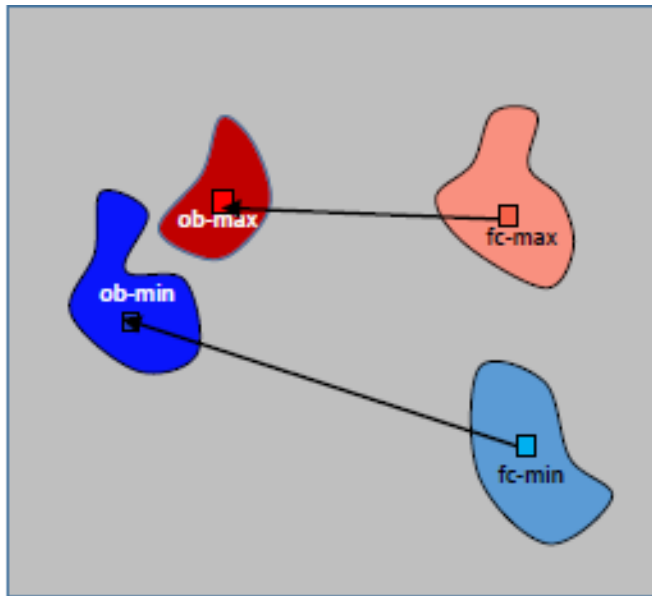
- **Motivation for verifying local extremes in a NWP model domain**
- **From motivation to the creation of a novel spatial verification scheme**
- **Computational methodology of new scheme:**
- **A forecast example**
- **Characteristics of new scheme relative to FSS and SAL spatial schemes**
- **Additional information**
- **Contact and References**

## MOTIVATION:

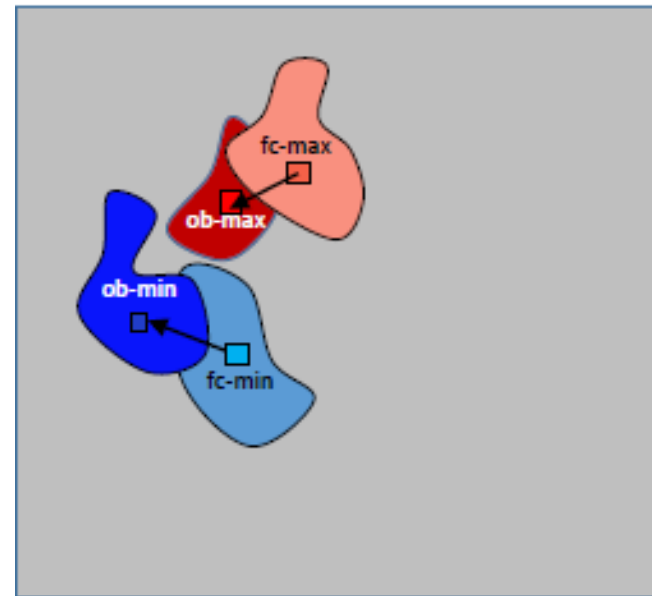
Figure 1a-b illustrate a challenging forecasting situation when NWP users experience significant spatial variability of precipitation (red area with observed maximum (ob-max), and blue area with observed minimum (ob-min) which could potentially be with zero precipitation ). The grey 'back-ground' value represents intermediate precipitation amounts.

The observed local extremes occur within close distance geographically. The lighter red and blue areas represent forecast highest and lowest values, respectively .

**It would be of great value, e.g. in the context of many types of outdoor activities, if both the wet extreme and the dry extreme could be forecasted with high accuracy , - regarding both absolute amount and spatial accuracy.**



**Fig.1a: non-optimal forecast** with relatively long distance ( represented by length of arrows) between forecasted and observed precipitation extremes (fc-max, ob-max, fc-min, ob-min )



**Fig.1b: Improved overlapping forecast** with relatively short distance ( represented by length of arrows) between forecasted and observed precipitation extremes (fc-max, ob-max, fc-min, ob-min )

# Transformation of MOTIVATION to a spatial verification scheme

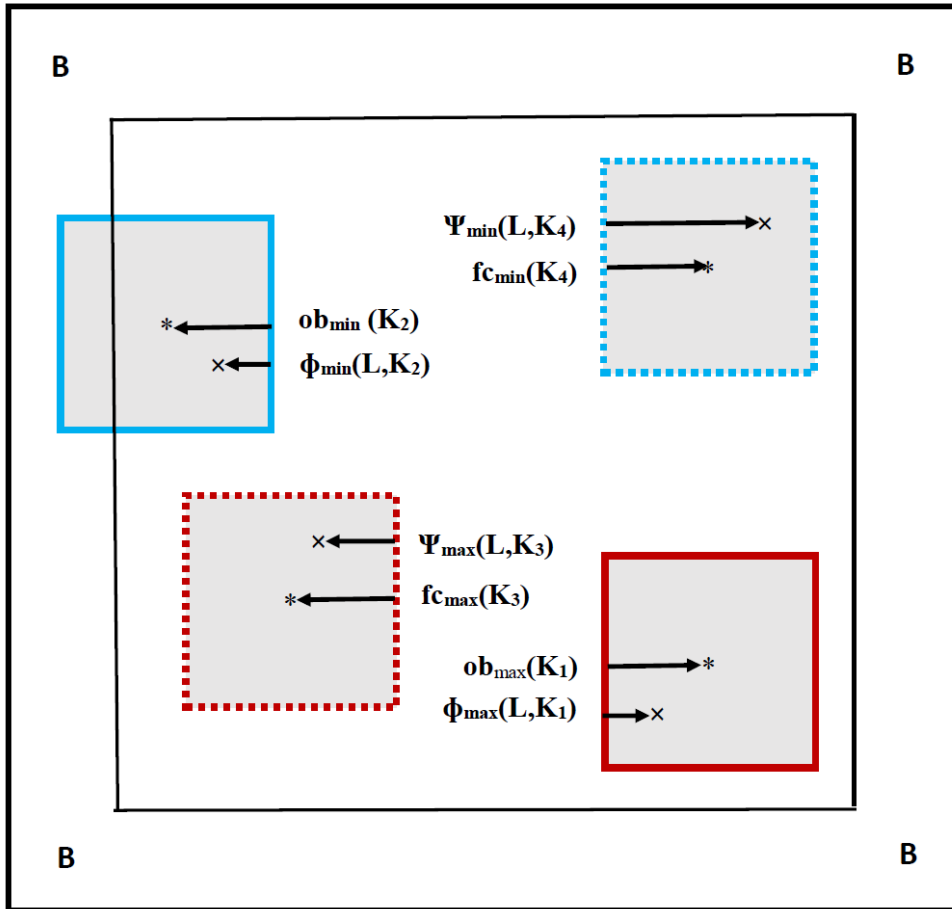
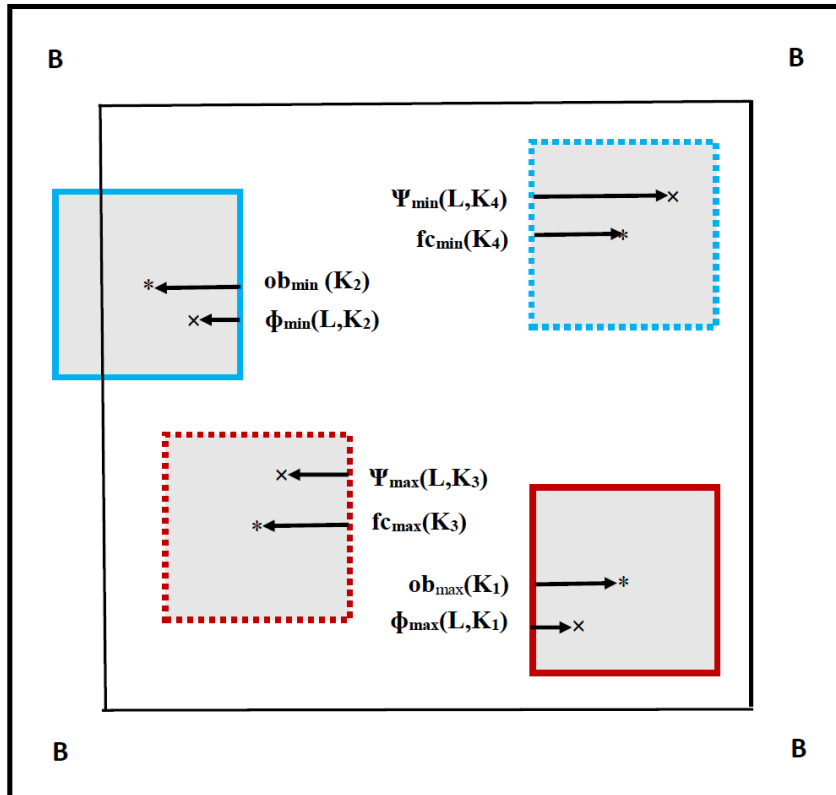


Fig.2 : Illustration of identified local extremes with neighborhoods of dimension L.

In case of multiple extreme points with  $\sim$  the same value  
 $1 \leq K_1 \leq M_1$ ,  $1 \leq K_2 \leq M_2$ ,  $1 \leq K_3 \leq M_3$ ,  $1 \leq K_4 \leq M_4$ ,  
 $M_1, M_2, M_3, M_4$  are the number of extremes of each type

## 'SLX' ( Structure of Local EXtremes )

- $ob_{max}(K_1)$  is maximum of the analysis field
- $\phi_{max}(L, K_1)$  is forecasted maximum in neighborhood of dimension L around  $ob_{max}(K_1)$
- $ob_{min}(K_2)$  is minimum of the analysis field
- $\phi_{min}(L, K_2)$  is forecasted minimum in neighborhood of dimension L around  $ob_{min}(K_2)$
- $fc_{max}(K_3)$  is maximum of the forecast field
- $\psi_{max}(L, K_3)$  is analyzed maximum in neighborhood of dimension L around  $fc_{max}(K_3)$
- $fc_{min}(K_4)$  is minimum of the forecast field
- $\psi_{min}(L, K_4)$  is analyzed minimum in neighborhood of dimension L around  $fc_{min}(K_4)$



## A spatial verification scheme 'SLX':

A boundary zone of width  $B$  is included to allow computations using full neighborhood size close to the lateral boundaries.

Alternatively, full neighborhoods are not feasible close to the lateral boundary points

**Example from Figure:  $ob_{max}(K_1)$ : Observed maximum , -  $K_1$  identifies extreme point, i.e. multiple number of extremes may be accounted for up to  $M_1$  – considered if highest values occur with almost identical values (small tolerance)**

**Maximum forecasted value in a neighborhood of dimension  $L$ :**

$$\Phi_{max}(L, K_1) = \text{Max}\{ \phi(i, j) \}, i \in [i_{K_1} - L, i_{K_1} + L], j \in [j_{K_1} - L, j_{K_1} + L]$$

$i_{K_1}, j_{K_1}$  are coordinates of the related forecasted values in central point.

## SLX

- *a novel scheme developed 2019-2020*
- *current application: precipitation fields*
- *input needed : decision on neighborhood size*
- *prerequisite : A score function is defined*



## ( Structure of Local EXtremes measures

- how does the forecast match identified local maxima of the analysis
- how does the identified local maxima of the forecast agree with the analysis
- how does forecast match identified local minima of the analysis, and finally
- how does the identified local minima of the forecast agree with the analysis.

i) , ii) , iii) , iv) represent separate comparisons leading to scores defined in interval  $[0, 1]$  :  $SLX(ob\_max)$ ,  $SLX(fc\_max)$ ,  $SLX(ob\_min)$ ,  $SLX(fc\_min)$

**Score function: 1 defines perfect match, 0 poor match between forecast and analysis in the neighborhood chosen.**

**Average computation for multiple extreme points**

**Also a weighted mean of the 4 score computations are carried out . This gives in total 5 outputs of a verification.**

# 'SLX' verification steps (1) :



The steps of the verification process for the score component  $SLX_{ob\_max}$  may be summarized as follows:

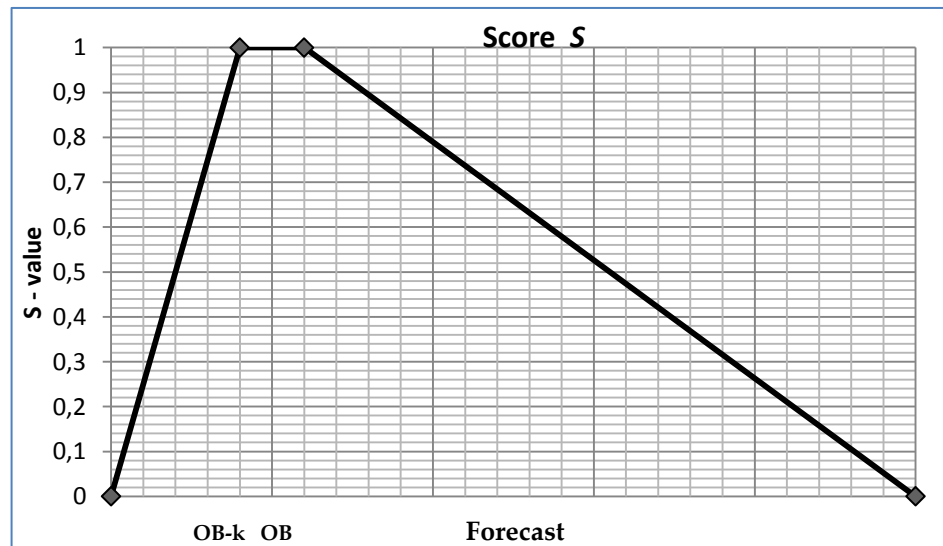
- I) Choose the current dimension of neighbourhood size  $L$  to be used for a given computation
- II) Determine the value (and positions in grid ) of the observed maxima  $ob_{max}(K_1)$
- III) Compute the forecasted maxima  $\phi_{max}(L, K_1)$  in the neighbourhood(s) of the extreme point(s).

## 'SLX' verification steps (2) :



IV) Insert the values  $ob_{\max}(K_1)$  as value = OB and  $\phi_{\max}(L, K_1)$  as a forecast to the score function  $S$  of Figure 3. The values and distance between the two determine the value between 0 and 1 of the score  $S_{ob_{\max}}(K_1)$

V) The procedure is repeated when multiple extreme points are diagnosed ,  $1 \leq K_1 \leq M_1$  and the average of all computations is computed as the final value of the score ( $SLX_{ob_{\max}}$ )



**Fig.3 Example of score function  $S$  which is asymmetric (developed in collaboration with professional NWP users)**

# 'SLX' verification scheme :

-

## SLX ( Structure of Local EXtremes ) measures:

Using these steps for each type of extreme leads to four individual scores defined in interval [0, 1] : SLX (ob\_max), SLX (fc\_max), SLX(ob\_min), SLX(fc\_min)

A weighted score SLX is computed as a combined score.

$$SLX_{ob\_max} = \frac{1}{M_1} \sum_{K_1=1}^{M_1} S_{ob\_max} (K_1)$$

$$SLX_{ob\_min} = \frac{1}{M_2} \sum_{K_2=1}^{M_2} S_{ob\_min} (K_2)$$

$$SLX_{fc\_max} = \frac{1}{M_3} \sum_{K_3=1}^{M_3} S_{fc\_max} (K_3)$$

$$SLX_{fc\_min} = \frac{1}{M_4} \sum_{K_4=1}^{M_4} S_{fc\_min} (K_4)$$

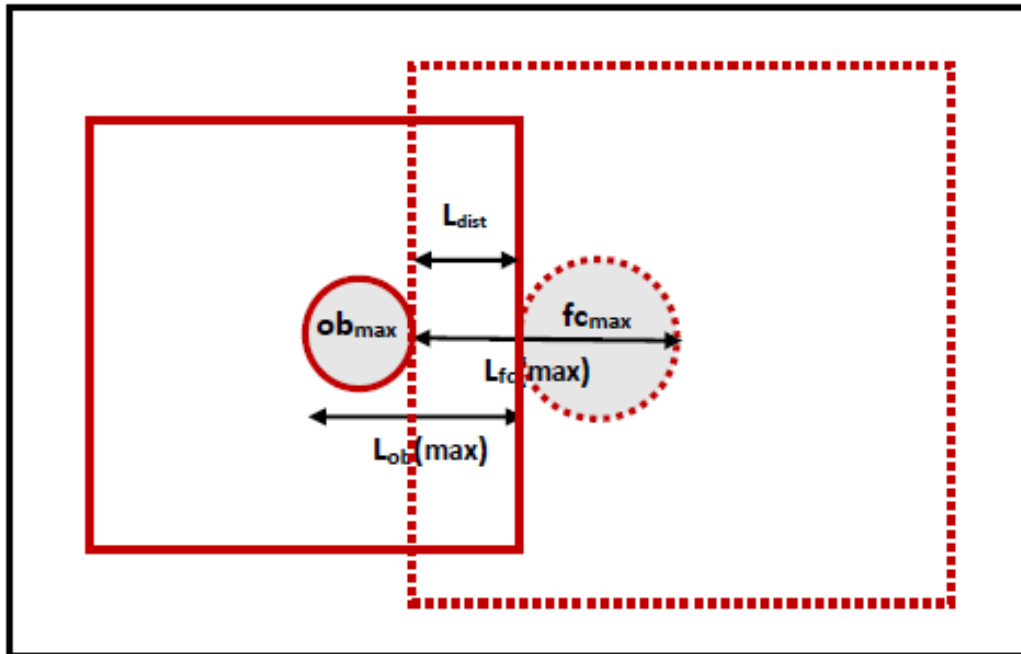
$$SLX = \frac{1}{4} ( SLX_{ob\_max} + SLX_{ob\_min} + SLX_{fc\_max} + SLX_{fc\_min} )$$



## ” Understanding SLX with multiple extreme points ”

Average computation:

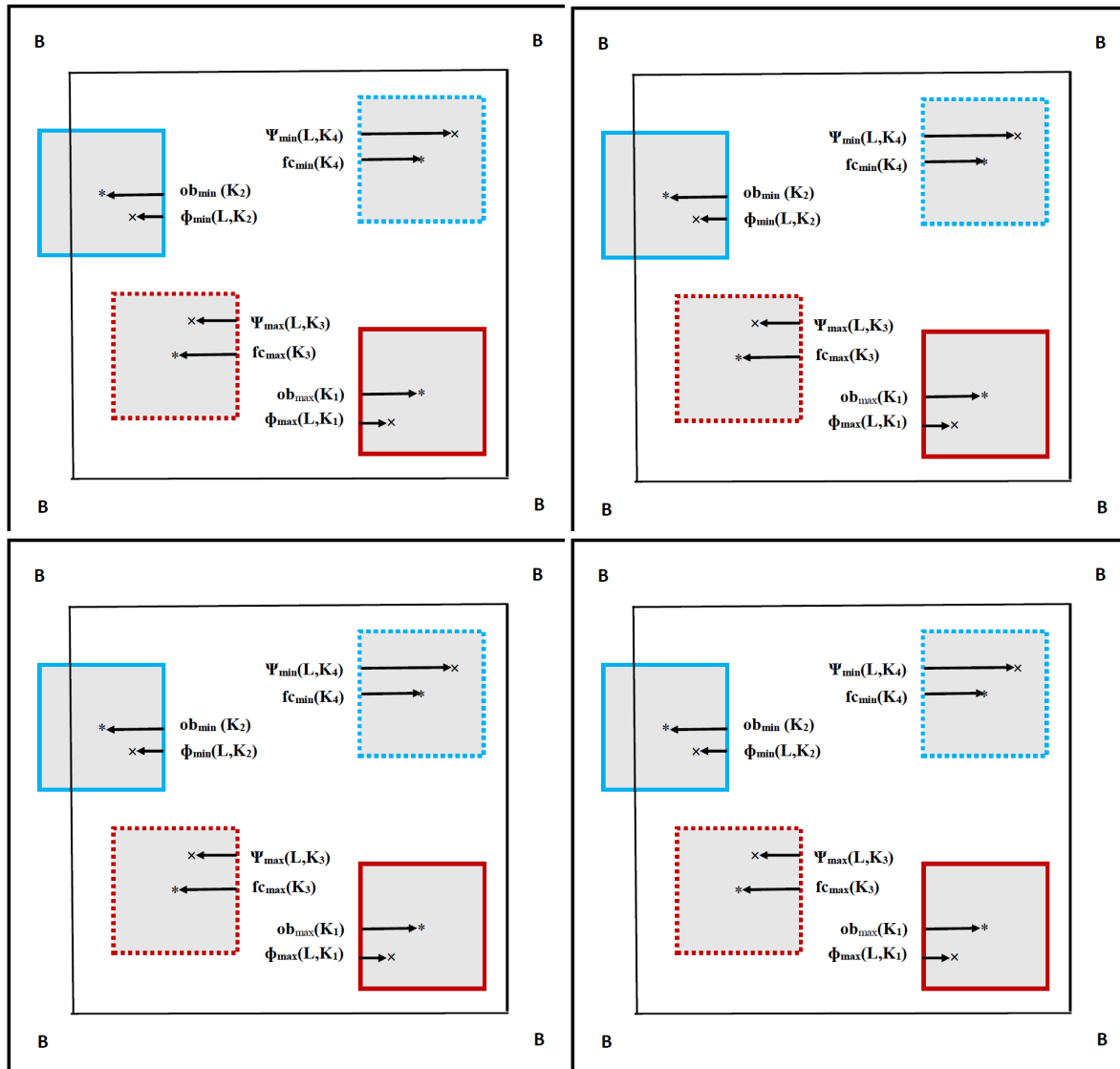
All extreme points are considered with equal weight in a neighborhood computation. The Figure illustrates situation for maxima. For minima an important option exists to look for a value closet to a specified value  $V_{\min}$  which may be larger than zero. This tends to prevent the score related with minima to become close to 1 in situations with large dry areas.



$$SLX_{ob\_max} = \frac{1}{M_1} \sum_{K_1=1}^{M_1} S_{ob\_max}(K_1)$$

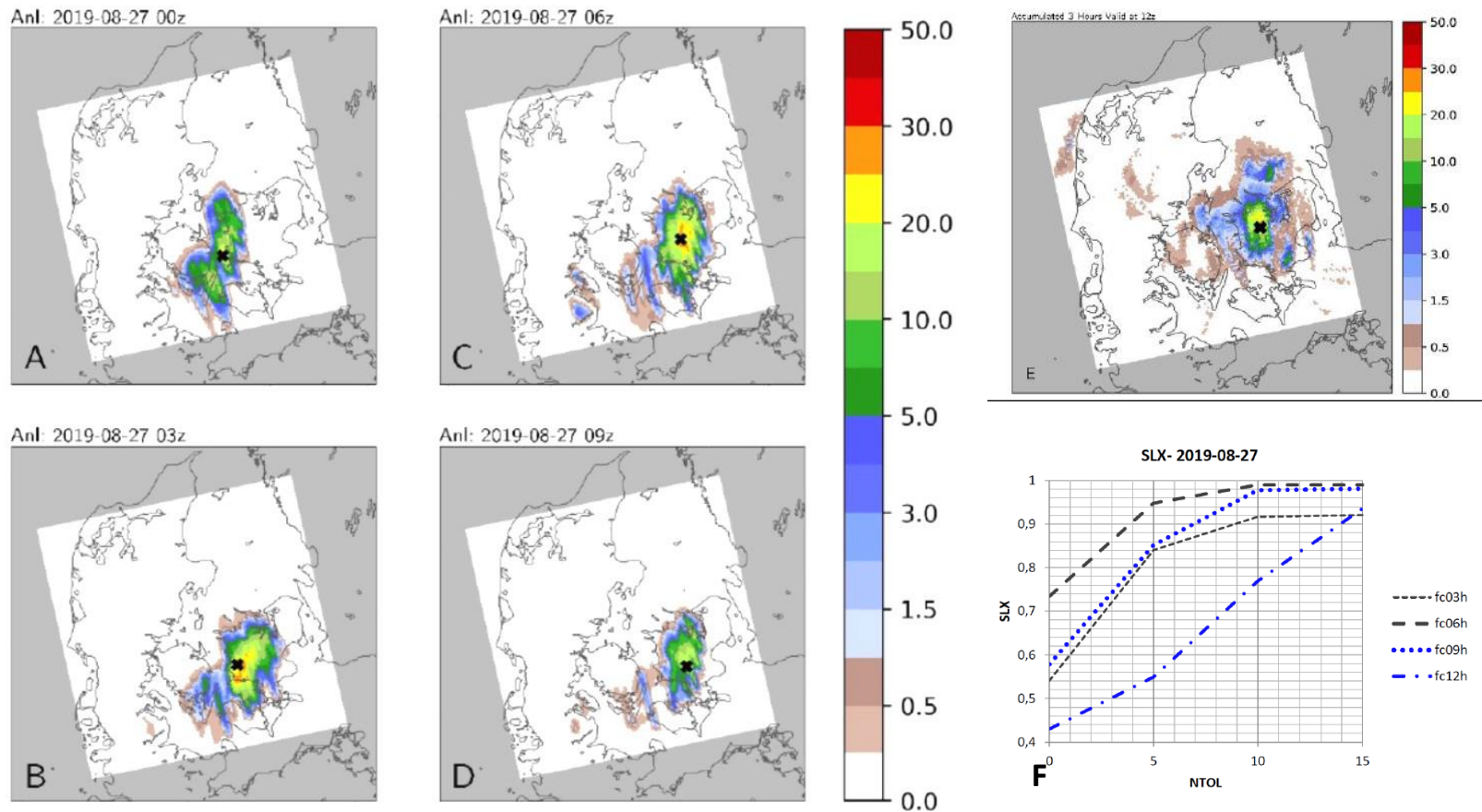
Fig. 4

Relation between neighborhood and score components : If  $ob_{\max} = fc_{\max}$  in grey colored areas and zero values apply outside, then  $S_{ob\_max} = S_{fc\_max}$  is zero for  $L < L_{dist}$ , which is the separation distance between  $ob_{\max}$  and  $fc_{\max}$  precipitation areas.  $L_{ob(max)}$  is a neighborhood size above which  $S_{ob\_max}$  becomes 1.  $L_{fc(max)}$  is a neighborhood size above which  $S_{fc\_max}$  becomes 1.



**Fig.5 For large domains multiple sub-areas may be included that can be treated with separate or combined statistics.**

# Forecast Example : Convection over parts of Denmark



**Fig. 6** Forecasted accumulated precipitation ( $\text{kg/m}^2$ ) valid from 9 UTC -12 UTC 27 August 2019 over the light squared areas of dimensions  $325 \text{ km} \times 325 \text{ km}$ . Figure A, B, C and D apply to forecasts starting at 00 UTC , 03 UTC , 06 UTC and 09 UTC respectively. Figure E shows the corresponding analyzed field of precipitation 9-12 UTC 27 August 2019. The black crosses indicate the maxima. Fig. 6 F shows the resulting combined scores of SLX , from four forecasts starting at different origin times.

## Basic comparisons with Fractions Skill Score (FSS) and SAL (Structure , Amplitude and Location)

CHARACTERISTICS	FSS	SAL	SLX
<b>Main characteristics of scheme</b>	Predict fractions correct , - Identify which scales can be resolved	Identify large-scale features, e.g. bias and variability of fields	Identify match of forecast and analysis around extreme values
<b>Number of score components</b>	<b>1</b>	<b>3</b>	<b>5</b>
<b>Type of spatial scheme</b>	<b>N</b>	<b>F</b>	<b>N + F</b>
<b>Dimensions (0-D, 1-D, 2-D) of input parameters in normal tests.</b>	<b>2-D</b> N- size and define Threshold/ percentile	<b>0-D</b> Uniquely defined once objects are fixed	<b>1-D</b> N-size + define Score- function between 0 and 1

**N=Neighborhood , F= Features based**

## Additional information

- An early version of the idea of verifying local extremes has been operational in DMI for several years (Sass and Yang 2012) . Some other relevant references are provided in the last slide. A publication on SLX is under review in an international journal.
- The scheme has been tested in many idealized cases and in a simulation of pre-operational conditions.
- The scheme has been prepared for operational use. An operational precipitation analysis in DMI makes this feasible from 2021.

# Contact information and References

## Contact:

Bent Hansen Sass, Danish Meteorological Institute , Lyngbyvej 100, 2100 , Copenhagen ,  
E-mail: [bhs@dmi.dk](mailto:bhs@dmi.dk) , Tel. +45 50 93 38 23

## References :

Gilleland, E., Ahijevych, D.A., Brown, B.G. and Ebert, E.E. 2010: Verifying Forecasts Spatially. *Bull. Amer. Meteor. Soc.*, October, 1365 – 1373.

Gilleland,E., Skok, G., Brown,G.B., Casati,B., Dorninger, M., Mittermaier, M.P., Roberts, N. and Wilson, L.J. 2020: A Novel Set of Geometric Verification Test Fields with Application to Distance Measures. *Mon. Wea. Rev.* **148**, 1653 - 1673

Roberts, N.M. and Lean, H.W. 2008: Scale-selective verification of rainfall accumulations from high-resolution forecasts of convective events. *Mon. Wea. Rev.*, **136**, 78-97.

Sass, B.H. and Yang, X. 2012: A verification score for high resolution NWP: Idealized and preoperational tests. HIRLAM Tech,Rep. No 69, 28 pp , Dec. 2012 , [Available from [www.hirlam.org](http://www.hirlam.org)]

Wernli, H., Paulat, M. 2008: SAL – A Novel Quality Measure for the Verification of Quantitative Precipitation forecasts. *Mon. Wea. Rev.*, **136**, 4470-4486